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Difference Operator Approach To Evaluate Integrals Involving Multiple Hypergeometric Functions Of Several Variable With Respect To Parameters

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In the present paper, making an appeal to difference operators, we evaluate certain integrals involving multiple hypergeometric functions of Chandel-Gupta (1986), Exton (1972,76), Karlsson (1986), Chandel and Gupa (2007) with respect to parameters. We also apply same technique to evaluate integrals involving hypergeometric functions of four variables due to Sharma and Parihar (1989). 2010 Mathematical Subject Classification : 33C50

Abstract

Keywords: Difference operator E, , Lauricella's Multiple hypergeometric functions, Appell's hypergeometric functions, Intermediate Lauricella multiple hypergeometric functions due to Karlsson.

Introduction

Recently, making an appeal to difference operator E, defined by

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(1.1)
$$E_{\alpha}f(\alpha) = f(\alpha+1), E_{\alpha}^{n}(f(\alpha)) = f(\alpha+n),$$

and integral due to Erdélyi [5.p.224]

(1.2)
$$\int_{-\pi}^{\pi} \frac{\sin[(m+1)\pi x] dx}{\sin \pi x \Gamma(\alpha_1 + x) \Gamma(\alpha_2 - x)} = \frac{2^{\alpha_1 + \alpha_2 - 2}}{\Gamma(\alpha_1 + \alpha_2 - 1)}, \quad Re(\alpha_1 + \alpha_2) > 1,$$

Joshi and Bhati [, Jnanaha 27 (1997)] evaluated some integrals involving hypergeometric functions of three and four variables and discussed some special cases.

Recently, making an appeal to difference operators Chandel [2003 presented ISAAC Congress 2003, York Univ. Toronto Canada] obtained various in transformations of multiple hypergeometric functions of several variables due to

Chandel-Gupta [, Jananaha 16 (1986)]. Chandel-Vishwakarma [, Janaha 19 (1989)] and discussed their interesting special cases.

In the present paper, making an appeal to difference operators, we evaluate certain interesting integrals involving multiple hypergeometric functions of several $F_{A}^{(n)}, F_{C}^{(n)}$

including Intermediate Lauricella's multiple hypergeometric variables functions and confluent form of Lauricella [16].

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